

# ERRATA - INTRODUCTION TO HAMILTONIAN DYNAMICAL SYSTEMS AND THE N-BODY PROBLEM

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- Pg 5, Ln -11:  $H(\phi(t, z_0)) < M$ .
- Pg 5, Ln -1:  $H = (\omega/2)(x^2 + u^2)$ .
- Pg 9, Fg B.4: Change ‘ $k$ ’ to ‘ $\kappa$ ’.
- Pg 10, Ln 1: Change ‘three’ to ‘two’.
- Pg 10, Ln 3: Change ‘four’ to ‘three’.
- Pg 10, Ln 9: Change ‘(1)’ to ‘(5)’.
- Pg 12, Ln 11: Change ‘ $\mathbf{R}^4$ ’ to ‘ $\mathbb{R}^4$ ’.
- Pg 15, Ln 18: Change ‘ $\mathbf{R}^3$ ’ to ‘ $\mathbb{R}^3$ ’.
- Pg 21, Eq 12:  $\dots, \dot{y} = -\frac{\partial H}{\partial x} = Kx + \frac{\partial U}{\partial x}$ .
- Pg 22, Ln 5: Pg 23 Ln -7: Change ‘polynomials’ to ‘functions’.
- Pg 26, Ln -6: Change ‘(C.11)’ to ‘(C.12)’.
- Pg 26, Eq 14:  $\dots, 0 = Ky + \frac{\partial U}{\partial x}$ ,
- Pg 29, Ln 10: Change ‘Siegal’ to ‘Siegel’.
- Pg 29, Pm 1.b: Change ‘brakcet’ to ‘bracket’.
- Pg 29, Pm 3.c:  $\dots, y = ksn(t, k)$
- Pg 30, Pm 5.c: Change ‘Sketch’ to ‘Sketch’.
- Pg 32, Pm 14: Change ‘ $+(3x_1^2 - \|x\|^2)$ ’ to ‘ $-\frac{1}{2}(3x_1^2 - \|x\|^2)$ ’
- Pg 32, Pm 14: Change ‘ $x_2$ ’ to ‘ $x_1$ ’
- Pg 39, Ln 14:  $(J^T O^T J)(J^T P^T J)$ .
- Pg 48, Ln 12:  $\gamma = 1/sqrt\{u, v\}$
- Pg 50, Lem 13: Change ‘ $(\gamma \pm \delta i)^{-1}$ ’ to ‘ $(\gamma \pm \delta i)^{\pm 1}$ ’.
- Pg 58, Lem 5: Change ‘any’ to ‘an’.
- Pg 59, Eq 5 change ‘ $u_2 = x_2 + \xi_2$ ’ to ‘ $u_2 = x_2 - \xi_2$ ’.
- Pg 67, Lem 1: *Let  $T$  be a real symplectic matrix. If  $T$  has a real logarithm, then  $T$  has a real symplectic logarithm.*
- Pg 71, Pm 16: Change ‘ $+(3x_1^2 - \|x\|^2)$ ’ to ‘ $-\frac{1}{2}(3x_1^2 - \|x\|^2)$ ’
- Pg 71, Pm 16: Change ‘ $x_2$ ’ to ‘ $x_1$ ’
- Pg 72, Ln 2: Change ‘his’ to ‘this’.
- Pg 82, Ln -2: Change ‘Poincarè’ to ‘Poincaré’.
- Pg 89, Eq 8:  $\dots + \frac{\partial \Xi}{\partial z}(t, z) J \frac{\partial^2 \Xi}{\partial t \partial z}(t, z) = 0, \dots$
- Pg 89, Thm 1: *A symplectic change of variables defined on a simply connected domain takes a Hamiltonian system into a Hamiltonian system.*
- Pg 91, Eq 3:

$$H = \sum_{i=1}^N \frac{\|v_i\|^2}{2m_i} - \dots$$

- Pg 99, Ln 10: Change ‘ $S_4$ ’ to ‘ $S_2$ ’.
- Pg 100, Eq 18:  $\dots, \dot{R} = \frac{\Theta^2}{r^3} - \frac{\mu}{r}, \dots$
- Pg 100, Eq 19:  $\ddot{r} = \dot{R} = \frac{c^2}{r^3} - \frac{\mu}{r^2}$

- Pg 100, Eq 20:  $\cdots = +c^2 u^3 - \mu u^2$ ,
- Pg 101, Eq 23:  $u_2 = (r_1 \cos \theta_1, r_1 \sin \theta_1), \cdots$
- Pg 101, Eq 24:  $H = \frac{1}{2M_2} \{\cdots\} + \frac{1}{2M_3} \{\cdots\} - \cdots$
- Pg 107, Ln 13: Change ‘in the paper’ to ‘in that paper’.
- Pg 130, Ln -1: Change ‘ $\xi$ ’ to ‘ $t$ ’.
- Pg 131, Ln 1: Change ‘ $\frac{\partial \phi}{\partial \zeta}$ ’, to ‘ $\frac{\partial \phi}{\partial \xi}$ ’, twice.
- Pg 131, Ln -3: Change ‘ $\partial g(T, \xi')/\partial \xi$ ’ to ‘ $\partial g(T, \xi')/\partial t$ ’
- Pg 133, Eq 6:

$$\dot{x} = y + x(1 - x^2 - y^2),$$

$$\dot{y} = -x + y(1 - x^2 - y^2),$$

- Pg 133, Eq 7:  $\dot{r} = r(1 - r^2), \cdots$
- Pg 133, Ln -6:  $\dot{r} = -2r$
- Pg 133, Ln -5,6: Change  $\exp -2\pi$  to  $\exp -4\pi$ .
- Pg 133, Ln -1: Change ‘III.A.2’ to ‘IV.A.2’.
- Pg 134, Eq 8: Change ‘ $\frac{\partial \phi(T, \xi)}{\partial \zeta}$ ’, to ‘ $\frac{\partial \phi(T, \xi)}{\partial \xi}$ ’,
- Pg 135, Ln 2: Change ‘IV.B.2’ to ‘V.C.1’.
- Pg 135, Ln -7: Change ‘IV.A.2’ to ‘V.C.4’.
- Pg 135, Ln -2: Change ‘III.A.2’ to ‘IV.A.2’.
- Pg 152, Pm 6: Change ‘ $(Tx) =$ ’ to ‘ $f(Tx) =$ ’.
- Pg 159, Ln -9: Change ‘ $y_2 + \mu$ ’ to ‘ $y_2 - \mu$ ’.
- Pg 159, Eq 1:  $H = \frac{\|y\|^2}{2} - x^T K y - \frac{\mu}{d_1} - \frac{1-\mu}{d_2} + \mu x_1 + \frac{3}{2}\mu^2$
- Pg 160, Eq 2:  $H = \epsilon^{-3} \left\{ \frac{\|\eta\|^2}{2} - \frac{c^2}{\|\xi\|} \right\} - \xi^T K \eta + O(\epsilon)$
- Pg 161, Ln 5:  $\|x\| \simeq \epsilon^2$
- Pg 167, Pm 4: Change ‘ $+(3x_1^2 - \|x\|^2)$ ’ to ‘ $-\frac{1}{2}(3x_1^2 - \|x\|^2)$ ’
- Pg 167, Pm 4: Change ‘ $x_2$ ’ to ‘ $x_1$ ’
- Pg 172, Ln 2: Change ‘(3)’ to ‘(1)’.
- Pg 172, Ln 13:  $H^* = G$
- Pg 172, Ln -6:

$$= \sum_{n=0}^{\infty} \left( \frac{\epsilon^n}{n!} \right) H_0^n(x)$$

- Pg 175, Eq 7:  $W_1 = I^2 \{2 \sin 2\phi + \frac{1}{4} \sin 4\phi\}$
- Pg 183, Ln -12: Change ‘ $H_1^0$ ’ to ‘ $H_i^0$ ’.
- Pg 184, Eq 10:  $\cdots = -(m_1 \lambda_1 + \cdots + m_{2n} \lambda_{2n})(s_1 x_1)^{m_1} (s_2 x_2)^{m_2} \cdots (s_{2n} x_{2n})^{m_{2n}}$
- Pg 184, Ln 8:  $\cdots$  the eigenvalues are  $-(m_1 \lambda_1 + \cdots + m_{2n} \lambda_{2n})$
- Pg 184, Eq 15:

$$\dot{y}_i = y_i D H^\#(y_1 y_{n+1}, \dots, y_n y_{2n})$$

$$\dot{y}_{i+n} = y_{i+n} D H^\#(y_1 y_{n+1}, \dots, y_n y_{2n})$$

- Pg 198, Eq 36: Change ‘ $4uv_{00}$ ’ to ‘ $4u_0 v_0$ ’.
- Pg 198, Eqs 38 & 39: Change ‘ $\beta/120$ ’ to ‘ $\beta/20$ ’
- Pg 199, Pm 2a: Change ‘ $\{H_0^1, W_1\}$ ’ to ‘ $\{H_1^0, W_1\}$ ’.
- Pg 199, Pm 2b:  $H^* = I + (3\gamma/8)I^2 + (17\gamma^2/32)I^3 + (5725\gamma/1024)I^4 + \cdots$
- Pg 200, Pm 8: Change ‘ $x_1$ ’ to ‘ $x_i$ ’ twice.
- Pg 211, Ln -13:  $\cdots$  to the 4-bifurcation point as  $\cdots$
- Pg 215, Ln -5: Change ‘ $\gamma \rightarrow \epsilon\gamma$ ’ to ‘ $A \rightarrow \epsilon A$ ’.

- Pg 219, Eq 2: Change  $A_0$  to

$$A_0 = \begin{pmatrix} 0 & \omega & 0 & 0 \\ -\omega & 0 & 0 & 0 \\ -\delta & 0 & 0 & \omega \\ 0 & -\delta & -\omega & 0 \end{pmatrix}$$

- Pg 219, Eq 7: Change  $B_0$  and  $B_1$  to

$$B_0 = \begin{pmatrix} -\omega i & 0 & 0 & 0 \\ 0 & \omega i & 0 & 0 \\ 0 & -\delta & \omega i & 0 \\ -\delta & 0 & 0 & -\omega i \end{pmatrix} \quad B_1 = \begin{pmatrix} -ai & 0 & 0 & b \\ 0 & ai & b & 0 \\ 0 & 0 & ai & 0 \\ 0 & 0 & 0 & -ai \end{pmatrix}$$

- Pg 220, Eq 8:  $\{\lambda^2 + (\omega + \nu a)^2\}^2 + 2\nu b\delta\{\lambda^2 - (\omega + \nu a)^2\} + \nu^2 b^2 \delta^2$ ,
- Pg 244 Ln 5 = 0 =  $\partial H_1(x, 1, t)/\partial x$ ,.
- Pg 249 Ln 15 Change ', that is,' to ',this is '.
- Pg 249 Ln -5  $X(f^{nm}(z_0)) < X(z_0) + m(r+1)$ .
- Pg 249 Ln -4  $X(f^{nm}(z_0)) \geq X(z_0) + mr$ .
- Pg 249 Ln -3  $\frac{X(z_0)}{nm} + \frac{m}{nm}r \leq \frac{X(f^{nm}(z_0))}{nm} \leq \frac{X(z_0)}{nm} + \frac{m}{nm}(r+1)$ .
- Pg 250 Ln 10 'Hence  $\lim_{n \rightarrow \infty} X(f^n(z_0))/n$  exists'.
- Pg 251 Ln 1 Change 'From Lemma 5 ' to 'From Lemma 4'.
- Pg 251 Ln 3  $X(z_n) + r \leq X(f^i(z_n)) < X(z_n) + r + 1$ .
- Pg 251 Ln 6  $X(z_n) + r - 1 \leq X(f^i(z_n)) \leq X(z_0) + r + 2$ .
- Pg 251 Ln -9  $f^q(z_n) = z_n + (p, 0)$ ,.
- Pg 253 Ln 17  $\rho_0 \leq p/q \leq \rho_1$ .
- Pg 257 Ln -8 Add to the end of condition (iv') "and a smooth arc connecting  $I^-(z_2)$  and  $I^+(z_1) \cup \{(x, 1) : x \in \mathbf{R}\}$ .
- Pg 258 Ln 10 ...must connect  $f(I^+(z_2)) \cup$ .
- Pg 258 Ln 13 ...intersecting  $f(I^+(z_1)) \cup f(I^-(z_2))$ .
- Pg 261 Fg. D.7 Change  $f$ 's to  $f^{i_1}$ 's and  $f^2$  to  $f^{i_2}$ 's.
- Pg 261 Fg. D.7 Caption Change to "Image of  $\{z : X(z) = X(z_1)\}$ ".
- Pg 261 Ln 1  $I^+(f^{i_2}(z_2)) \cup \{(x, 1)x >$ .
- Pg 263 Ln -18 Change 'a continuum' to 'a set'.
- Pg 263 Ln -16 Change 'a continuum' to 'a set'.
- Pg 264 Ln 22  $Y(f(x_0 + (i+1)p/q, y_{i-1}))$ .
- Pg 264 Ln 23 Add to the right hand side  $+(x_0 + ip/q, 0)$ .
- Pg 264 Ln 24 Add to the right hand side  $+(x_0 + ip/q, 0)$ .
- Pg 264 Ln 25 Change 'extending' to 'extended'.
- Pg 267 Ln 20 Change last word ('the') to 'which is the'.
- Pg 271 Ln 2 Change 'determine if it has' to 'i.e., find'.
- Pg 272 Ln -7 Change 'comparing' to 'compared'.
- Pg 273 Ln 10 Change  $p/g$  to  $p/q$ .
- Pg 275 Ln 5 Change 'lurid' to 'lucid'.
- Pg 277 Ln 15 Change 'Melss' to 'Meiss'.
- Pg 278 Ln 5 (i)  $h(x+1, xt+1) = h(x, xt)$ .
- Pg 281, Ln 8: Change 'Chrikov' to 'Chirikov'.
- Pg 281, Ln 27: Change 'Mech. 72, 173-179.' to 'Mech. 1, 12-30.'
- Pg 282, Ln 15: Change 'Eelements' to 'Elements'.